



## 2nd Int. Workshop on Multi-Level Modelling



An algebraic instantiation technique  
illustrated by multilevel design patterns

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# Outline

- **Practical motivation**
  - › Multi-level meta-modelling propriety solutions in modern telecom management
- **Theoretical motivation**
  - › Juan de Lara's SoSyM paper on multi-level meta-modelling patterns
- **Dynamic Multi-Layer Algebra**
  - › Theoretical introduction (structure, functions, bootstrap, dynamic instantiation)
  - › Examples (syntax with compact notation)
- **Multi-level meta-modelling patterns**
  - › Type-Object pattern
  - › Dynamic Features

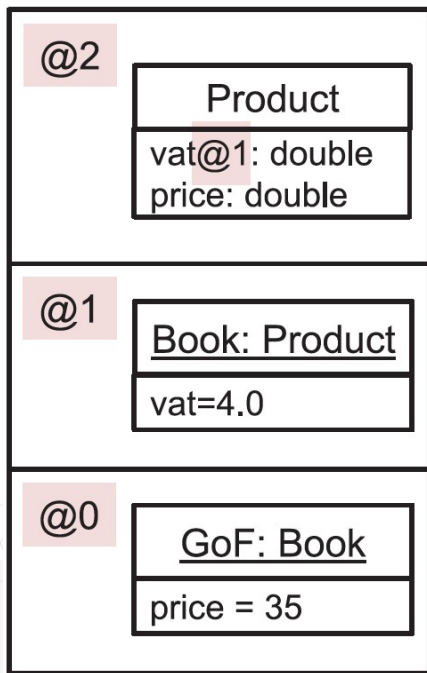
# Practical Motivation

- **Modern telecom network management is getting more centralised**
  - › Network devices are managed via Software Defined Networking (SDN)
  - › Network services are virtualised and managed as Virtual Network Functions (VNF)
  - › Global service orchestrators keep all data in model-based repositories
  - › Model manipulation indirectly influences the operation of complex multi-operator, multi-vendor, multi-technology services and devices in the physical network and data centres
  - › Complex telecom services are gradually created by stake-holders in an ecosystem
  - › Model-based orchestration solutions must support both design- and run-time modelling
  - › Flexible management of modelled elements is needed
  - › Model repositories not only store instances, but also keep references to their types
- **Modelling in telecom management must be DevOps-enabled**

# Theoretical Motivation

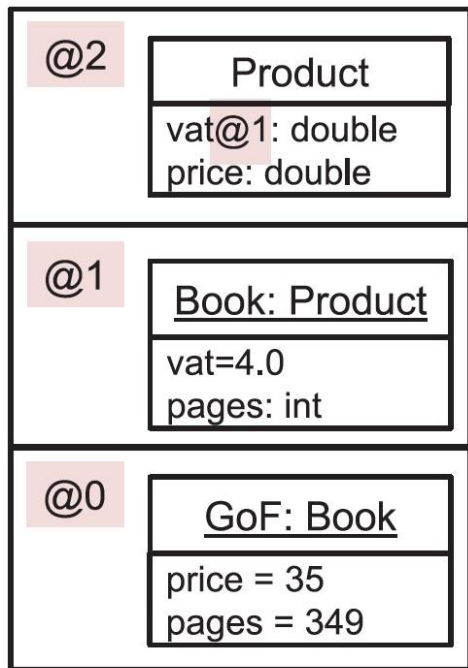
- **Instantiation is key operation between model and meta-model levels**
- **Linguistic instantiation is well-established by current methodologies**
- **Ontological meta-modelling is carried out by architects at design-time**
- **Combined linguistic and ontological model design may become complex**
- **Instantiation can also connect design-time and run-time models**
- **Complex software ecosystems may require partial instantiation by steps**
- **Multi-level instantiation support by potency notion is generic**
- **The levelling of partial instantiation is to be pre-defined in potency**

# Theoretical Motivation (Type-Object pattern)



- **Intent:**
  - › Explicit modelling of types and their instances
  - › Types can be added dynamically
  - › Types define features that are known a priori
  - › Instances concretise type features
- **Usage:**
  - › Model-based telecom management systems for
    - » flexible introduction of new types on demand
    - » establishment of 3-level modelling for devices (device kind -> device type -> device instance)

# Theoretical Motivation (Dynamic Features)



- **Intent:**
  - › Adding new features to existing types
  - › Instances can concretise new features
- **Usage:**
  - › Model-based telecom management systems for
    - » flexible extension of types on demand
    - » supporting type ecosystems among various tools (multiple stake-holders handle devices differently and independently of each other)

# Dynamic Multi-Layer Algebra

- **Concepts**

- › Formal definition (ASM based)
- › Dynamic (partial) instantiation
- › Extendable initialisation

- **Components**

- › Modelling structure and functions
- › Built-in constructs (Bootstrap)
- › Dynamic instantiation mechanism

# Data Representation (Labels)

## Labelled Directed Graph (Nodes, Edges, Labels)

- Both Nodes and Edges can have following Labels:
  - › **ID**: globally unique ID of model entity
  - › **Name**: name of model entity
  - › **Cardinality**: cardinality of model entity
  - › **Meta**: ID of meta-model entity
  - › **Value**: value of model entity (used only for attributes)
  - › **Attributes** (children): list of attributes
    - » Attributes are virtual nodes with the root as a model element (complex tree structure)



# Data Representation (Universes)

## Superuniverse $|\mathcal{U}|$ of a state $\mathcal{U}$ of Dynamic Multi-Layer Algebra

- Universes defined:
  - ›  $U_{\text{Bool}}$ : contains logical values {true/false}
  - ›  $U_{\text{Number}}$ : contains rational numbers  $\{\mathbb{Q}\}$  and infinity  $\infty$
  - ›  $U_{\text{String}}$ : contains character sequences of finite length
  - ›  $U_{\text{ID}}$ : contains all the possible entity IDs
  - ›  $U_{\text{Basic}}$ : contains elements from  $\{U_{\text{Bool}} \cup U_{\text{Number}} \cup U_{\text{String}} \cup U_{\text{ID}}\}$
- All universes contain **undef** representing an undefined value

# Data Representation (Labels + Universes)

## Labels of entities take values from universes

- Entity  $X$  has following Name-Value mappings
  - ›  $X_{\text{Name}}: U_{\text{String}}$
  - ›  $X_{\text{ID}}: U_{\text{ID}}$
  - ›  $X_{\text{Meta}}: U_{\text{ID}}$
  - ›  $X_{\text{Cardinality}}: [U_{\text{Number}}, U_{\text{Number}}]$
  - ›  $X_{\text{Value}}: U_{\text{Basic}}$
  - ›  $X_{\text{Attrib}}: U_{\text{ID}}[]$

**Example:**  $\text{Book}_{\text{ID}}=42, \text{Book}_{\text{Meta}}=123, \text{Book}_{\text{Cardinality}}=[0, \infty], X_{\text{Value}}= \text{undef}, \text{Book}_{\text{Attrib}}=[]$

Compact notation: **{"Book", 42, 123, [0, inf], undef, []}**

# ASM Functions (Shared Functions)

## Shared functions: represent model entity (current) configuration

- › Can be modified either by algebra or environment (e.g.  $X_{IDConcreteObjec} := X_{NewMetaDefinition}$ )
- $Name(ID): \begin{cases} name, if \exists X: X_{ID} = ID \wedge X_{Name} = name \\ undef, otherwise \end{cases}$
- $Meta(ID): \begin{cases} Y_{ID}, if \exists X, Y: X_{ID} = ID \wedge X_{Meta} = Y_{ID} \\ undef, otherwise \end{cases}$
- $Card(ID): \begin{cases} [low, high], if \exists X: X_{ID} = ID \wedge \\ X_{Cardinality} = [low, high] \\ undef, otherwise \end{cases}$
- $Value(ID): \begin{cases} val, if \exists X: X_{ID} = ID \wedge X_{Value} = val \\ undef, otherwise \end{cases}$
- $Attrib(ID, Idx): \begin{cases} attrib, if \exists X, i: X_{ID} = ID \wedge \\ X_{Attrib}[Idx] = attrib \\ undef, otherwise \end{cases}$

# ASM Functions (Derived Functions)

## Derive functions: represent calculations

- › Cannot change the model
- › Only obtain or restructure existing information

- $Contains(ID_1, ID_2): \begin{cases} true, if \exists c, idx: c = Attrib(ID_1, idx) \wedge \\ (c_{ID} = ID_2 \vee Contains(c_{ID}, ID_2)) \\ false, otherwise \end{cases}$
- $DeriveFrom(ID_1, ID_2): \begin{cases} true, \exists x, y: x_{ID} = ID_1 \wedge \exists y: y_{ID} = ID_2 \\ \wedge (x_{Meta} = y \vee DeriveFrom(x_{Meta}, y)) \\ false, otherwise \end{cases}$

# Built-in Constructs (Basic Types)

## Basic entities (“reification” of DMLA’s universes)

- › Entities required to represent basic types for Meta (otherwise  $X_{\text{Meta}}: U_{\text{ID}}$  in ASM by default)
- **Bool** :-  $U_{\text{Bool}}$
- **Number** :-  $U_{\text{Number}}$
- **String** :-  $U_{\text{String}}$
- **ID** :-  $U_{\text{ID}}$
- **Basic** :-  $U_{\text{Basic}}$ 
  - › Bool, Number, String and ID inherit from Basic (Note:  $U_{\text{Basic}} = \{U_{\text{Bool}} \cup U_{\text{Number}} \cup U_{\text{String}} \cup U_{\text{ID}}\}$ )
  - › Other basic types such as Date, Double etc. could be introduced similarly

# Principal Entities

- **Attribute:**
  - › {“Attribute”, ID<sub>Attribute</sub>, ID<sub>Attribute</sub>, [0, inf], undef, [{“Attributes”, ID<sub>Attributes</sub>, ID<sub>Attribute</sub>, [0, inf], undef,[]} ] }
- **AttribType:**
  - › {“AttribType”, ID<sub>AttribType</sub>, ID<sub>Attribute</sub>, [0, 1], undef, [{“AType”, ID<sub>AType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>ID</sub>,[]} ] }
- **Node:**
  - › {“Node”, ID<sub>Node</sub>, ID<sub>Node</sub>, [0, inf], undef, [{“Attributes”, ID<sub>Attributes</sub>, ID<sub>Attribute</sub>, [0, inf], undef,[]} ] }
- **Edge:**
  - › {“Edge”, ID<sub>Edge</sub>, ID<sub>Edge</sub>, [0, inf], undef, [{“Attributes”, ID<sub>Attributes</sub>, ID<sub>Attribute</sub>, [0, inf], undef,[]}, {“EdgeSrc”, ID<sub>EdgeSrc</sub>, ID<sub>Src</sub>, [1, 1], ID<sub>Node</sub>,[]}, {“EdgeTrg”, ID<sub>EdgeTrg</sub>, ID<sub>Trg</sub>, [1, 1], ID<sub>Node</sub>,[]} ] }
  - › {“Src”, ID<sub>Src</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [{“SrcType”, ID<sub>SrcType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>Node</sub>,[]} ] }
  - › {“Trg”, ID<sub>Trg</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [{“TrgType”, ID<sub>TrgType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>Node</sub>,[]} ] }

# Principal Entities (Attribute-like)

- **Attribute:**

- › {“Attribute”,  $ID_{Attribute}$ ,  $ID_{Attribute}$ , [0, inf], undef,  
[  
    {“Attributes”,  $ID_{Attributes}$ ,  $ID_{Attribute}$ , [0, inf], undef,[]}  
]  
}

- **AttribType:**

- › {“AttribType”,  $ID_{AttribType}$ ,  $ID_{Attribute}$ , [0, 1], undef,  
[  
    {“AType”,  $ID_{AType}$ ,  $ID_{AttribType}$ , [0, 1],  $ID_{ID}$ ,[]}  
]  
}

Note:  $ID_{ID}$  refers to Basic Types

# Principal Entities (Type-like)

- **Node:**

- › {“Node”, **ID<sub>Node</sub>**, **ID<sub>Node</sub>**, [0, inf], undef, [{"Attributes", **ID<sub>Attributes</sub>**, **ID<sub>Attribute</sub>**, [0, inf], undef,[]} ]}

- **Edge:**

- › {“Edge”, **ID<sub>Edge</sub>**, **ID<sub>Edge</sub>**, [0, inf], undef,

- [

- {“Attributes”, **ID<sub>Attributes</sub>**, **ID<sub>Attribute</sub>**, [0, inf], undef,[]},

- {“EdgeSrc”, **ID<sub>EdgeSrc</sub>**, **ID<sub>Src</sub>**, [1, 1], **ID<sub>Node</sub>**,[]},

- {“EdgeTrg”, **ID<sub>EdgeTrg</sub>**, **ID<sub>Trg</sub>**, [1, 1], **ID<sub>Node</sub>**,[]}

- ]

- › {“Src”, **ID<sub>Src</sub>**, **ID<sub>Attribute</sub>**, [1, 1], undef, [{"SrcType”, **ID<sub>SrcType</sub>**, **ID<sub>AttribType</sub>**, [0, 1], **ID<sub>Node</sub>**,[]} ]}

- › {“Trg”, **ID<sub>Trg</sub>**, **ID<sub>Attribute</sub>**, [1, 1], undef, [{"TrgType”, **ID<sub>TrgType</sub>**, **ID<sub>AttribType</sub>**, [0, 1], **ID<sub>Node</sub>**,[]} ]}



# Entity Examples

- **Simple Attribute:**

- › attr String Age
- › {“Age”, ID<sub>AgeAttribute</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [{“AgeType”, ID<sub>AgeType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>Number</sub>, []] }

- **Complex Attribute:**

- › complex Name { attr String FirstName, attr String LastName }
- › {“Name”, ID<sub>Name</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [  
  {“FirstName”, ID<sub>FirstName</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [{“FNType”, ID<sub>FNType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>String</sub>, []] } }  
  {“LastName”, ID<sub>LastName</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [{“LNType”, ID<sub>LNType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>String</sub>, []] } } ] }

# Dynamic Instantiation

- Structure definition and bootstrap represent models as states of DMLA
- Instantiation can create many different instances of the same type without violating meta definition constraints
- Model manipulation may result in valid or invalid models
- Instantiation is checked by formulae (Helper & Validation Formulae)
  - › Helper formula example:  
$$\varphi_{CardinalityCheck}(C, I): \neg \text{DeriveFrom}(I, \text{ID}_{\text{Attribute}}) \vee \text{Card}(\text{Meta}(I))[0] \leq \text{Count}(a: \exists i: a = \text{Attrib}(C, i) \wedge \varphi_{InstCounter}(I, a) \leq \text{Card}(\text{Meta}(I))[1])$$
  - › Validation formula example:  
$$\varphi_{EntityIns}(I, M): \{\exists c, \text{idx}: \text{Attrib}(I, \text{idx}) = c \wedge \varphi_{IsValid}(c, \text{Meta}(c))\} \vee \text{Value}(I) \neq \text{undef}$$
- Instantiation procedure verifies formulae after each partial instantiation

# Instantiation Procedure

- Iterative process
- Instantiates at least one entity (e.g. attribute) in each step
- Based on annotated attributes and principal entities
- Consists of instructions having abstract selector and action functions
- Verifies 7 instantiation validation formulae

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Algorithm    The instantiation algorithm

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- 1: **rule** Instantiate(ID\_SubjectEntity, Instructions)
  - 2: **for all**  $\lambda_{selector}, \lambda_{action}$  in Instructions **do**
  - 3:    **for all** SelectedEntity in  $\lambda_{selector}$ (ID\_SubjectEntity) **do**
  - 4:         $\lambda_{action}$ (SelectedEntity)
-

# Instantiation Examples

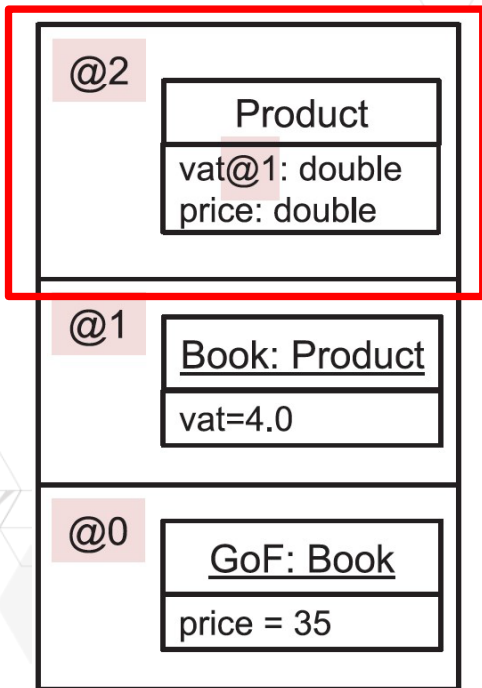
- **Simple attribute:**

- › {“Age”, ID<sub>AgeAttribute</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [{“AgeType”, ID<sub>AgeType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>Number</sub>, []} ]}
- » {“Age”, ID<sub>ConcreteAgeAttribute</sub>, ID<sub>AgeAttribute</sub>, [1, 1], 23, []}

- **Complex attribute:**

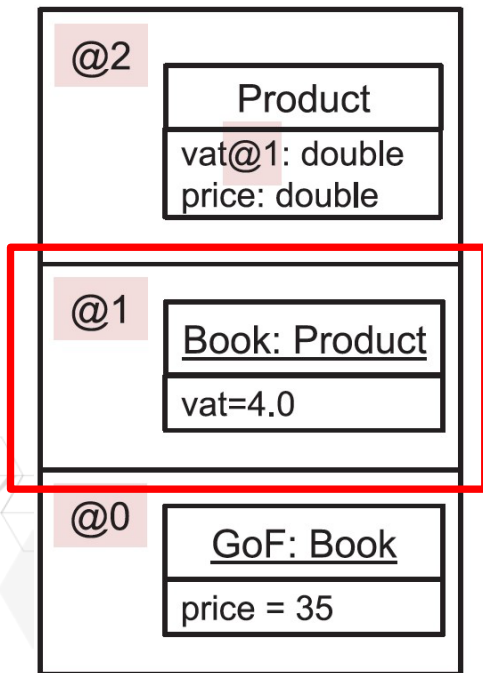
- › {“Name”, ID<sub>Name</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [  
  {“FirstName”, ID<sub>FirstName</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [{“FNType”, ID<sub>FNType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>String</sub>, []} ]}  
  {“LastName”, ID<sub>LastName</sub>, ID<sub>Attribute</sub>, [1, 1], undef, [{“LNType”, ID<sub>LNType</sub>, ID<sub>AttribType</sub>, [0, 1], ID<sub>String</sub>, []} ]} ]}
- » {“ConcreteName”, ID<sub>ConcreteName</sub>, ID<sub>Name</sub>, [1, 1], undef, [  
  {“FirstName”, ID<sub>ConcreteFirstName</sub>, ID<sub>FirstName</sub>, [1, 1], “John” ,[]}  
  {“LastName”, ID<sub>ConcreteLastName</sub>, ID<sub>LastName</sub>, [1, 1], “Smith” ,[]} ]}

## Type-Object pattern (Level 2)



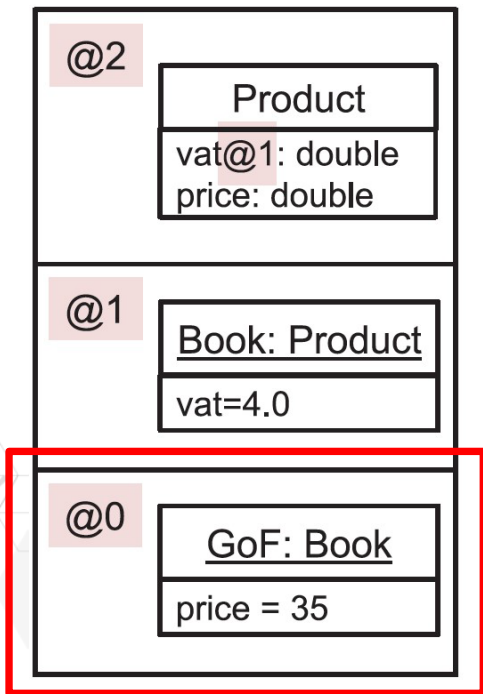
```
{“Product”, IDProduct, IDNode, [0, inf], undef,  
[  
  {“vat”, IDVat, IDAttribute, [1, 1], undef,[  
    {“vatType”, IDVatType, IDAttribType, [0, 1], IDNumber, []},  
  
    {“price”, IDPrice, IDAttribute, [1, 1], undef,[  
      {“priceType”, IDPriceType, IDAttribType, [0, 1], IDNumber, []}  
    ]  
  ]  
}
```

# Type-Object pattern (Level 1)



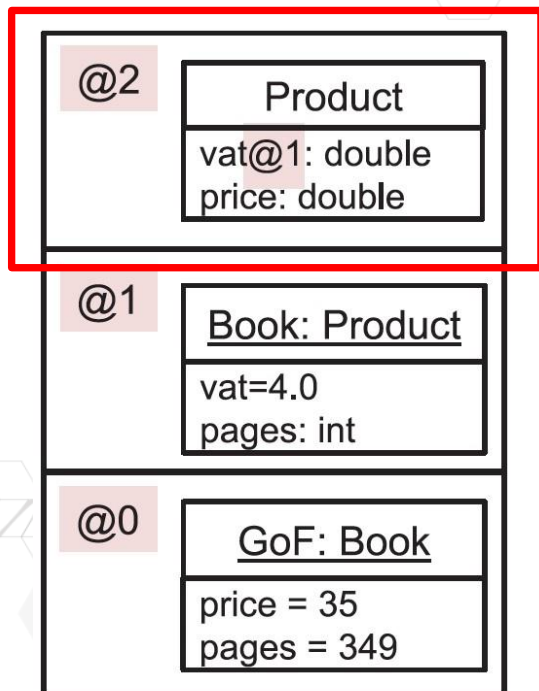
```
{“Book”, IDBook, IDProduct, [0, inf], undef,  
 [  
   {“vat”, IDConcreteVat, IDVat, [1, 1], 4,[]},  
   {“price”, IDPrice, IDAttribute, [1, 1], undef,[  
     {“priceType”, IDPriceType, IDAttribType, [0, 1], IDNumber, []}  
   ]  
 }
```

# Type-Object pattern (Level 0)



```
{“GoF”, ID_ConcreteBook, ID_Book, [0, inf], undef,  
 [  
   {“vat”, ID_ConcreteVat, ID_Vat, [1, 1], 4, []},  
   {“price”, ID_ConcretePrice, ID_Price, [1, 1], 35, []}  
 ]  
 }
```

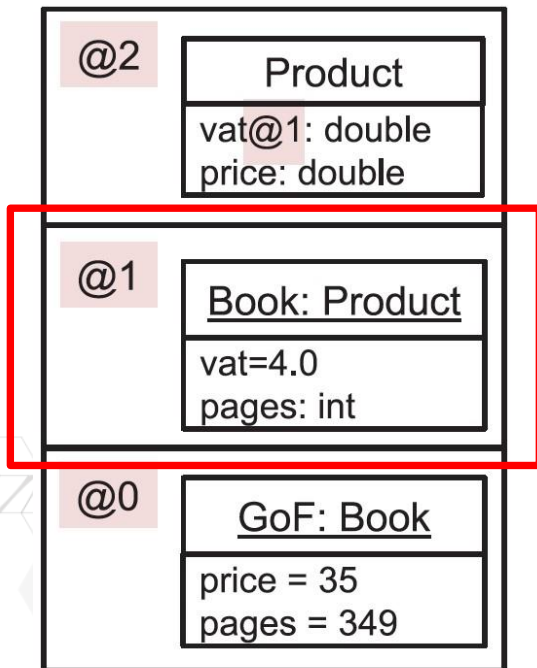
## Dynamic Features (Level 2)



```
{“Product”, IDProduct, IDNode, [0, inf], undef,  
[  
  {“vat”, IDVat, IDAttribute, [1, 1], undef,[  
    {“vatType”, IDVatType, IDAttribType, [0, 1], IDNumber, []},  
    {“price”, IDPrice, IDAttribute, [1, 1], undef,[  
      {“priceType”, IDPriceType, IDAttribType, [0, 1], IDNumber, []},  
      {“Attributes”, IDAttributes, IDAttribute, [0, inf], undef,[]}  
    ]  
  ]  
}
```

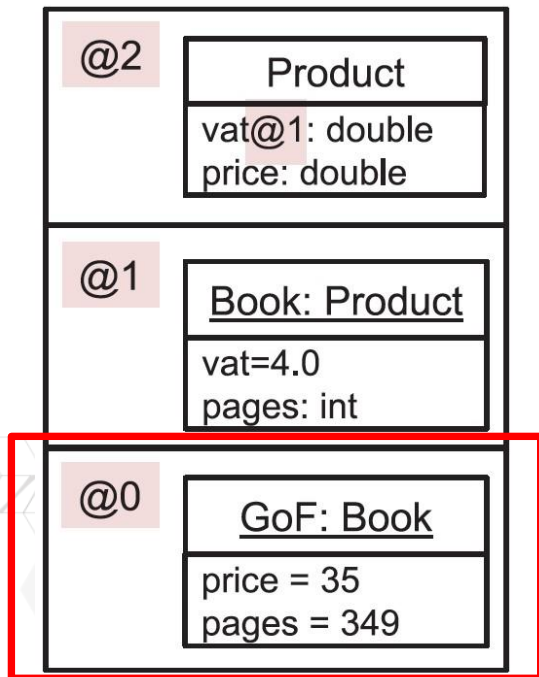


# Dynamic Features (Level 1)



```
{“Book”, IDBook, IDProduct, [0, inf], undef,  
[  
    {“vat”, IDConcreteVat, IDVat, [1, 1], 4, []},  
  
    {“price”, IDPrice, IDAttribute, [1, 1], undef,[  
    {“priceType”, IDPriceType, IDAttribType, [0, 1], IDNumber, []},  
  
    {“pages”, IDPages, IDAttribute, [1, 1], undef,[  
    {“pagesType”, IDPagesType, IDAttribType, [0, 1], IDNumber, []}  
]  
}
```

# Dynamic Features (Level 0)



```
{“GoF”, ID_ConcreteBook, ID_Book, [0, inf], undef,  
[  
    {“vat”, ID_ConcreteVat, ID_Vat, [1, 1], 4, []},  
    {“price”, ID_ConcretePrice, ID_Price, [1, 1], 35, []},  
    {“pages”, ID_ConcretePages, ID_Page, [1, 1], 349, []}  
]  
}
```

# Summary & Future Work

- **Multi-level meta-modelling patterns are well-known, but used in proprietary implementation in design-time & run-time**
- **Dynamic Multi-Layer Algebra is a novel multi-level modelling approach**
  - › Precise semantics – defined in ASM notation
  - › Flexible constraints – can work with customised Bootstrap entities
  - › Dynamic instantiation – abstract selector and action functions (black-box approach)
  - › Platform and implementation independent – portable DMLA executor possible
- **Multi-level meta-modelling patterns can be expressed in DMLA**
- **Future work**
  - › Experiment with various bootstraps (e.g. reified selectors, operators, *node-edge equality*)
  - › Implementation of self-referring DMLA (reified implementation entities in bootstrap)



# Thank You!



# Any Questions?